

PROOF OF $(*x, y|R : P) = (*y, x|R : P)$

Fill in the reasons for the following proof. Let z be a variable that does not occur in P or R .

$$\begin{aligned} & (*x, y|R : P) \\ = & \\ & (*x| : (*y|R : P)) \\ = & \\ & (*x| : (*y|R : (*z|(z = y) : P))) \\ = & \\ & (*x| : (*y, z|R \wedge (z = y) : P)) \\ = & \\ & (*x| : (*y| : (*z|R \wedge (z = y) : P))) \\ = & \\ & (*y| : (*x| : (*z|R \wedge (z = y) : P))) \\ = & \\ & (*y| : (*x, z|R \wedge (z = y) : P)) \\ = & \\ & (*y| : (*x|R : (*z|(z = y) : P))) \\ = & \\ & (*y| : (*x|R : P)) \\ = & \\ & (*y, x|R : P) \end{aligned}$$